$n \int \Gamma \left[ los \left( \frac{\Theta}{n} + \frac{360k}{n} \right) + lsin \left( \frac{\Theta}{n} + \frac{360k}{n} \right) \right]$ 

Graphing  $(r, \theta) \rightarrow \text{graph } \theta$  first, then r

- If r > 0, 2pi <= θ < 4pi, do (r, θ + 2pi)
- If r > 0,  $-2pi \le \theta \le 0$ , do  $(r, \theta 2pi)$
- If r < 0, 0<= θ < 2pi, do (-r, θ + pi)
- $X = r \cos \theta$ ,  $Y = r \sin \theta$
- Pol to Rec  $\rightarrow$  remember X = r cos  $\theta$ , Y = r sin  $\theta$
- Rec to Pol  $\rightarrow$  find r =  $\sqrt{x^2 + y^2}$  AND  $\theta$  = tan^-1 (x/y)
- Equ to Pol to Rec  $\rightarrow$  make one side into rcos $\theta$  or rsin $\theta$  (multiplying by r), and then complete the square
- Equ to Rec to Pol  $\rightarrow$  just plugin X = r cos  $\theta$ , Y = r sin  $\theta$  and solve (you'll get trig values = #)
- R = # MEANS its a circle. Θ = angle MEANS line through (0,0). Y= rsinθ MEANS hor line. X =rcosθ MEANS vert line.

## MAKE TABLE FOR ALL, PLUG IN VALUES

IF sin AND + +, - + graph on pos y-axis IF cos AND + +, - + graph on pos x-axis IF cos AND - -, + - graph on neg x-axis Cardioid: a(1±cosθ) and a(1±sinθ) Limacon without loop: a±bcosΘ and a±bsinΘ AND a>b Limacon with loop: a±bcosΘ and a±bsinΘ AND b>a Rose: r=acos(bΘ)and r=asin(bΘ). IF b=even number, petals = 2b. IF b=odd number, petals = b Lemniscates: r^2 = a^2 sin(2Θ) and r^2 = a^2 cos(2Θ). PROPELLER type

Complex  $\{a(\cos xi + \sin xi)\}$  to rectangular $\{a+bi\} \rightarrow multiply$  it out Polar $\{a+bi\}$  to complex  $\rightarrow$  find r, find theta

Multiplying complex numbers: multiply outside numbers, and add the angles together Dividing complex numbers: divide outside numbers, and subtract the angles

[r (cosθ+isinθ)]^n → r^n[cos(nθ)+isin(nθ)] (a+bi)^n → convert to complex, do step directly above Complex roots (look at image given)

Unit vector/ "same-direction" vector: a/ sqrt (a<sup>2+b</sup>) i + b/ sqrt (a<sup>2+b</sup>) i and  $\Theta$  = tan<sup>-1</sup> (y/x)

(Plane problem with Plane velocity, plane direction, wind velocity, wind direction AKA GROUNDSPEED): ALWAYS write I before J

- 1. Find Va = Velocity of plane (#j if going straight)
- 2. Find Vw = Velocity of jet stream. Convert all to 0-180 range. Ex: N30W = 120 degrees. "Northeasternly" = 45 degrees.
- 3. Find Vg = Velocity relative to ground = Va + Vw
- 4. Find Actual speed = magnitude of Vg = Square root of Vg components squared
- 5. Find Angle of bearing = 90- inverse tangent (J / I) (use the j and i from Vg)

How much does it weigh problems:

- 1. Given: angle of incline of ramp, force to push object. Find: how much object weighs
- 2. Sin (angle) = force to push/ how much it weighs

Cable Tension Problems (ROUND TO FOUR DIGITS):

- 1. Left→ ||F1|| (DO NOT MAKE #) \* [cos(180-left\_angle)i + sin(180-left\_angle)j]
- 2. Right→ ||F2|| (DO NOT MAKE #) \* [cos(right\_angle)i + sin(right\_angle)j]
- 3. Down  $\rightarrow$  pounds\*j
- 4. Left + Right + Down = 0
- 5. You'll get (A||F1||+B||F2||)i + (C||F1||+D||F2||-E) = 0. Use first equation (The one with A and B) to solve for ||F2|| = # ||F1||.
- 6. Substitute into second equation, solve to GET ||F1||, then solve to GET ||F2|| using ||F2|| = # ||F1||

 $\begin{aligned} r &= \frac{6}{1 - \cos \theta} \\ r &= 6 + r \cos \theta \\ r^2 &= \chi^2 + 12 \times + 36 \\ \# + y^2 &= \# + 12 \times + 36 \\ y^2 &= 12 (\chi + 3) \end{aligned}$ 

One thing pulling two other things (truck pulling two other trucks):

1. Always draw angle on graph (rotate). You'll get bottom force(i) +  $\frac{1}{2}$  top force sqrt2 (i) +  $\frac{1}{2}$  top force sqrt2 (j) = F= ANS

Coefficient of friction = (object weight)sin(angle of incline)/(object weight)cos(angle of incline)

Dot product = multiply i parts, multiply j parts, multiply k parts, and ADD to get one number Angle between vectors =  $cos\theta$  = (dot product)/(magnitude of u)(magnitude of v)

Decomposing vectors into orthogonal vectors:

1.  $V1 = (v * w) / ||w||^2$  times w (as vector) REMEMBER:  $||w|| = sqrt\{A^2 + B^2\}$ . V2 = V - V1Parallel vectors  $\rightarrow$  multiples of each other Orthogonal  $\rightarrow$  dot product is 0

Given vectors, find y so that angle between vectors is  $\theta$ :

- 1. Dot product is going to be  $a1a2+b1+b2 \rightarrow #+#y$
- 2. Find magnitudes. Ur going to get sqrt(#) and sqrt(#+y^2)

3. Substitute,  $\cos of \theta$  (num) = (dot product)/ (mag of u \* mag of v). BUTTERFLY, SQUARING, CHECK BOTH ANSWERS

Find acute angle... unit vector...x-axis...[given distance], [given work]

1. Find PO = Position Vector. You'll get [given work] = #cosθ. SOLVE USING INVERSE COS

Finding force to keep an object still on a ramp:

- 1. Fg = -(weight)j w (the parallel force) = cos(angle)i + sin(angle)j
- 2. [-weight\*sin(angle)] / [MAGNITUDE SQUARED] = magnitude of v = ANS

Work (2D and 3D):

- 1. force\* (cos  $\theta i$  + sin  $\theta i$ ) = #(#i + #j)  $\rightarrow$  distance(i) \* #(#i + #j)  $\rightarrow$  (i) is ans. Since we don't have another j, no j component
- 2. F = Divide all of Ai + Bj + Ck with mag ( $sqrt[A^2+b^2+C^2]$ ) to get new vector, attach newton in front of the new vector
- 3. PO = Position vector (use the coordinates given)
- 4. Multiply F and PO (multiply the i's together, multiply the j's and then the k's and then add)

Incline Problems:

Sin (the angle given) = ||F2|| / ||F1||

F2 = force required to hold object still on the ramp, the little vector of new triangle, given in POUNDS = pounds\* sin(angle) F1 = force of gravity, weight of object, the straight-down vector of new triangle = pounds\*cos(angle)

River with width, river's speed, [\_] mph boat Problems, HOW MUCH TIME TO CROSS?:

- Vw = Velocity of boat relative to water = diagonal line
- Vc = Velocity of water = laying on x-axis

Vd = Velocity of boat that's going to the opposite side= laying on y-axis

- 1. Find vector Vc = [river current]i + 0j
- 2. Solve for A: -[river current] = [given velocity of boat]cosA. Subtract 90 to get direction angle (ANS)
- 3. To find out how long it takes: (river width) / [given velocity of boat] = sqrt [(-[river current])^2 + B^2]

Calculate direction angles of a 3D vector: cos^-1 [A(or B or C)/ sqrt (A^2 + B^2 + C^2)] (DO FOR A B AND C) Calculate direction ANGLE or a 3D vector...

Ex: vector v makes angle of a = pi/3 with pos x-axis and b = pi/3 with positive y-axis and ACUTE angle e with the z-axis. Find e. Use the formula  $cos^2 a + cos^2 b + cos^2 e = 1$ 

You'll get  $(\frac{1}{2})^2 + (\frac{1}{2})^2 + \cos^2 e = 1$ 

Then you'll get  $\cos^2 e = \frac{1}{2} == e$  can equal pi/4 OR 3pi/4. BUT we know it has to be ACUTE, so it's going to be pi/4